

Pensans' Written Method Calculation Policy



Written September 2023
Review September 2024

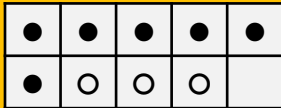
Addition Formal Written Methods For Calculation

Year 1

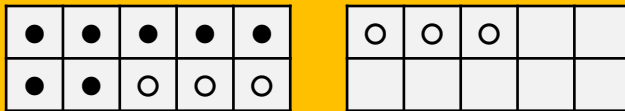
Add two one-digit numbers and a two-digit and one-digit number with a total less than 20.

- Solid circles for the first addend, hollow circles for the second.
- Solid represents RED Hollow represents YELLOW
- Fill in the Tens Frames top row first, from the left.

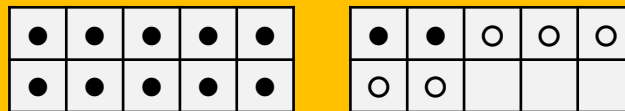
Example: $6 + 3 = 9$



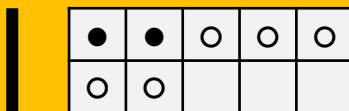
Example: $7 + 6 = 13$



Example (two frames): $12 + 5 = 17$



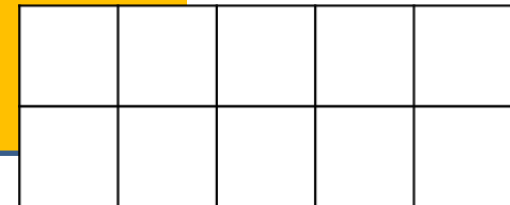
Example (tens and ones): $12 + 5 = 17$



Resources:

- Tens Frames
- Two sided counters
- Dienes

Practical first!



Year 2

Add ones to a two-digit number.

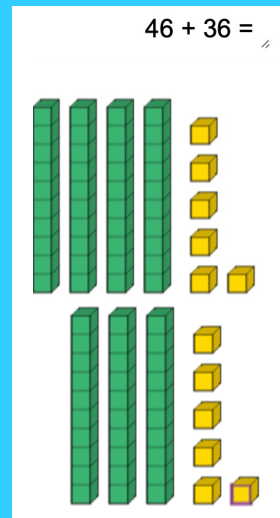
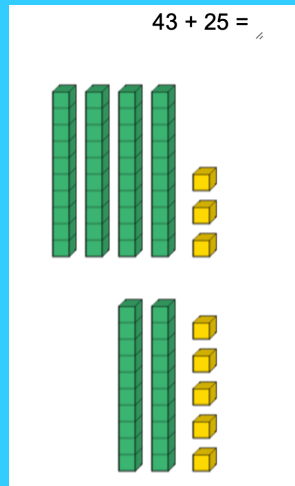
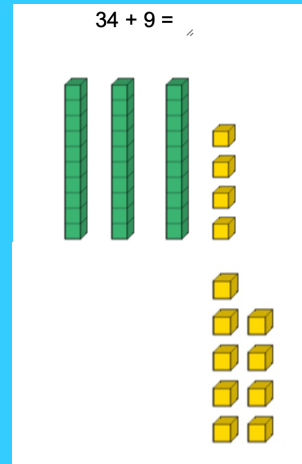
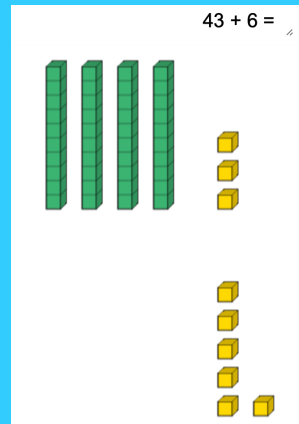
Add tens to a two-digit number.

Add one two-digit number to another.

Resources:

- Dienes

Addition Formal Written Methods for Calculation

Practical + Pictorial**Abstract****Short Column Written Method**

Two-digit + one-digit (not going over 10)

Example $43 + 6 = 49$

$$\begin{array}{r} 43 \\ + 06 \\ \hline 49 \end{array}$$

Two-digit + one-digit (going over 10)

Example $34 + 9 = 43$

$$\begin{array}{r} 34 \\ + 09 \\ \hline 43 \end{array}$$

Two-digit + two-digit (not going over 10)

Example $43 + 25 = 68$

$$\begin{array}{r} 43 \\ + 25 \\ \hline 68 \end{array}$$

Two-digit + two-digit (going over 10)

Example $46 + 36 = 82$

$$\begin{array}{r} 46 \\ + 36 \\ \hline 82 \end{array}$$

Year 3

Add numbers with up to 3 digits using formal written methods of columnar addition.

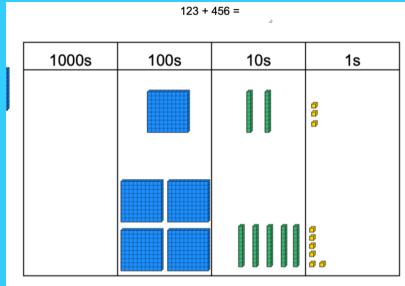
Resources:

- Dienes

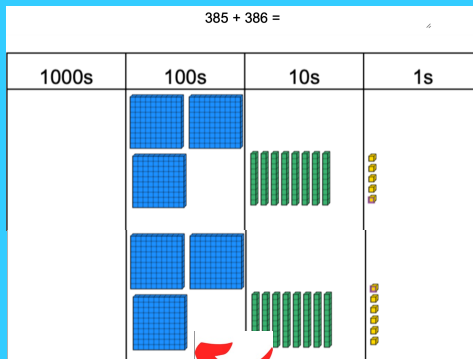
Addition Formal Written Methods for Calculation

Practical + Pictorial

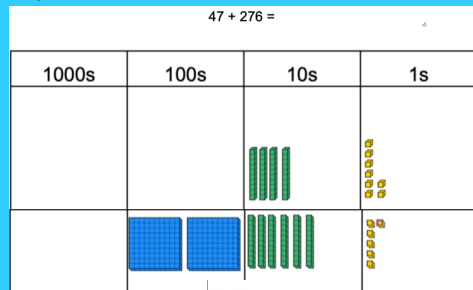
a) $123 + 456 = 579$



b) $385 + 386 = 771$



c) $47 + 276 = 323$



Abstract

Short Column Written Method

3-digit + 3-digit

a) $123 + 456 = 579$

$$\begin{array}{r} 123 \\ + 456 \\ \hline 579 \end{array}$$

b) $385 + 386 = 771$

$$\begin{array}{r} 385 \\ + 386 \\ \hline 771 \end{array}$$

Mixed 2-digit + 3-digit

c) $47 + 276 = 323$

$$\begin{array}{r} 047 \\ + 276 \\ \hline 323 \end{array}$$

Year 4

Add numbers with up to 4 digits using the formal written methods of columnar addition.

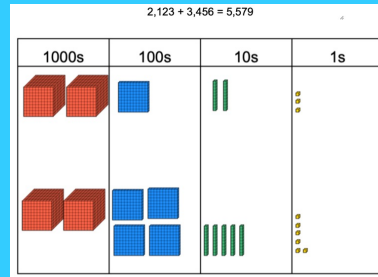
Resources:

- Dienes
- Place Value Mats (Progressive)

Addition Formal Written Methods for Calculation

Practical + Pictorial

$$a) 2,123 + 3,456 = 5,579$$



$$b) 3,456 + 5,289 = 8,745$$

Thousands	Hundreds, Tens and Ones			Decimals	
Thousands 1,000	Hundreds 100	Tens 10	Ones 1	Tenths 0.1	Hundredths 0.01
3	4	5	6		
5	2	8	9		
8	7	4	5		

$$c) 7,777 + 8,888 = 16,665$$

Thousands	Hundreds, Tens and Ones			Decimals	
Thousands 1,000	Hundreds 100	Tens 10	Ones 1	Tenths 0.1	Hundredths 0.01
7	7	7	7		
8	8	8	8		
1	6	6	6	5	

Abstract

Short Column Written Method

4-digit + 4-digit

$$a) 2,123 + 3,456 = 5,579$$

$$\begin{array}{r} 2\ 1\ 2\ 3 \\ +\ 3\ 4\ 5\ 6 \\ \hline 5\ 5\ 7\ 9 \end{array}$$

$$b) 3,456 + 5,289 = 8,745$$

$$\begin{array}{r} 3\ 4\ 5\ 6 \\ +\ 5\ 2\ 8\ 9 \\ \hline 8\ 7\ 4\ 5 \\ \hline \downarrow\ \downarrow \end{array}$$

$$c) 7,777 + 8,888 = 16,665$$

$$\begin{array}{r} 7\ 7\ 7\ 7 \\ +\ 8\ 8\ 8\ 8 \\ \hline 1\ 6\ 6\ 6\ 5 \\ \hline \downarrow\ \downarrow\ \downarrow\ \downarrow \end{array}$$

Don't forget mixed 3-digit + 4-digit

Year 5 + 6

Add whole numbers with more than 4 digits including using formal written methods (columnar addition).

Practise adding decimals including a mix of whole numbers and decimals, decimals with different numbers of decimal places and compliments of 1 e.g $0.17 + 0.83 = 1$.

Resources:

Place Value Mats (Progressive)

National curriculum expectations

Addition

Addition Formal Written Methods for Calculation

Practical + Pictorial

a) $52,849 + 18,423 = 71,272$

Millions			Thousands			Hundreds, Tens and Ones			Decimals		
Hundred Millions 100,000,000	Ten Millions 10,000,000	Millions 1,000,000	Hundred thousands 100,000	Ten thousands 10,000	Thousands 1,000	Hundreds 100	Tens 10	Ones 1	Tenths 0.1	Hundredths 0.01	Thousandths 0.001
						5	2	8	4	9	
						1	8	4	2	3	
						7	1	2	7	2	

c) $12.49 + 18.75 = 31.24$

Millions			Thousands			Hundreds, Tens and Ones			Decimals		
Hundred Millions 100,000,000	Ten Millions 10,000,000	Millions 1,000,000	Hundred thousands 100,000	Ten thousands 10,000	Thousands 1,000	Hundreds 100	Tens 10	Ones 1	Tenths 0.1	Hundredths 0.01	Thousandths 0.001
									1	2	
						1	8		4	9	
						3	1		2	4	

d) $108.4 + 5.756 = 114.156$

Millions			Thousands			Hundreds, Tens and Ones			Decimals		
Hundred Millions 100,000,000	Ten Millions 10,000,000	Millions 1,000,000	Hundred thousands 100,000	Ten thousands 10,000	Thousands 1,000	Hundreds 100	Tens 10	Ones 1	Tenths 0.1	Hundredths 0.01	Thousandths 0.001
						1	0	8		4	
						0	0	5		7	5
						1	1	3		1	5

Abstract

Short Column Written Method

More than 4-digit + 4-digit whole numbers

a) $52,849 + 18,423 = 71,272$

$$\begin{array}{r}
 52849 \\
 + 18423 \\
 \hline
 71272 \\
 \hline
 \end{array}$$

b) $2,668,777 + 2,776,899 = 5,445,676$

$$\begin{array}{r}
 2668777 \\
 + 2776899 \\
 \hline
 5445676 \\
 \hline
 \end{array}$$

Decimals

(Same number of decimal places)

c) $12.49 + 18.75 = 31.24$

$$\begin{array}{r}
 12.49 \\
 + 18.75 \\
 \hline
 31.24 \\
 \hline
 \end{array}$$

Decimals

(Different number of decimal places)

d) $108.4 + 5.756 = 114.156$

$$\begin{array}{r}
 108.400 \\
 + 005.756 \\
 \hline
 114.156 \\
 \hline
 \end{array}$$

Add in place holders to 'box' the addition.

Don't forget mixed digit whole number questions

Addition Formal Written Methods for Calculation

National curriculum expectations

Addition

Column method

Year 2

Add up to 2 two-digit numbers.

2-digit + 2-digit

$$43 + 25 = 68$$

$$\begin{array}{r} 43 \\ + 25 \\ \hline 68 \end{array}$$

$$46 + 36 = 82$$

$$\begin{array}{r} 46 \\ + 36 \\ \hline 82 \\ \hline \end{array}$$

$$47 + 76 = 123$$

$$\begin{array}{r} 47 \\ + 76 \\ \hline 123 \\ \hline \end{array}$$

Year 3

Add numbers with up to 3 digits using formal written methods of columnar addition.

3-digit + 3-digit

$$123 + 456 = 579$$

$$\begin{array}{r} 123 \\ + 456 \\ \hline 579 \end{array}$$

$$385 + 386 = 771$$

$$\begin{array}{r} 385 \\ + 386 \\ \hline 771 \\ \hline \end{array}$$

Year 4

Add numbers with up to 4 digits using the formal written methods of columnar addition.

4-digit + 4-digit

$$2,123 + 3,456 = 5,579$$

$$\begin{array}{r} 2123 \\ + 3456 \\ \hline 5579 \end{array}$$

$$3,456 + 5,289 = 8,745$$

$$\begin{array}{r} 3456 \\ + 5289 \\ \hline 8745 \\ \hline \end{array}$$

$$7,777 + 8,888 = 16,665$$

$$\begin{array}{r} 7777 \\ + 8888 \\ \hline 16665 \\ \hline \end{array}$$

Year 5 and Year 6

Add whole numbers with more than 4 digits including using formal written methods (columnar addition).

Practise adding decimals including a mix of whole numbers and decimals, decimals with different numbers of decimal places and compliments of 1 e.g $0.17 + 0.83 = 1$.

More than 4-digit + 4-digit

$$52,849 + 18,423 = 71,272$$

$$\begin{array}{r} 52849 \\ + 18423 \\ \hline 71272 \\ \hline \end{array}$$

$$2,668,777 + 2,776,899 = 5,445,676$$

$$\begin{array}{r} 2668777 \\ + 2776899 \\ \hline 5445676 \\ \hline \end{array}$$

Decimals (Same number of decimal places)

$$12.49 + 18.75 = 31.24$$

$$\begin{array}{r} 12.49 \\ + 18.75 \\ \hline 31.24 \\ \hline \end{array}$$

Decimals (Different number of decimal places)

$$108.4 + 5.756 = 114.156$$

$$\begin{array}{r} 108.400 \\ + 005.756 \\ \hline 114.156 \\ \hline \end{array}$$

Add in place holders to 'box' the addition.

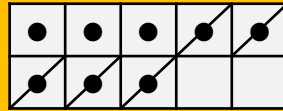
Subtraction Formal Written Methods For Calculation

Year 1

Subtract one-digit and two-digit numbers to 20, including zero.

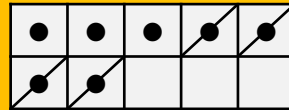
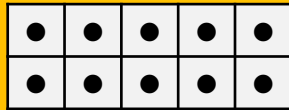
- Draw the starting number in **solid** circles and then cross out the amount you are taking away.
- Solid represents RED
- Fill in the Tens Frames top row first, from the left.

One-digit subtract one-digit Example: $8 - 5 = 3$



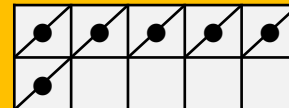
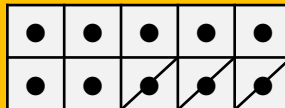
Two-digit subtract one-digit (not crossing ten)

Example: $17 - 4 = 13$



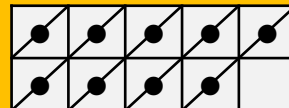
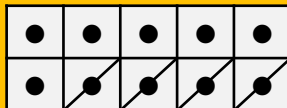
Two-digit subtract one-digit (crossing ten)

Example: $16 - 9 = 7$



Two-digit subtract two-digit

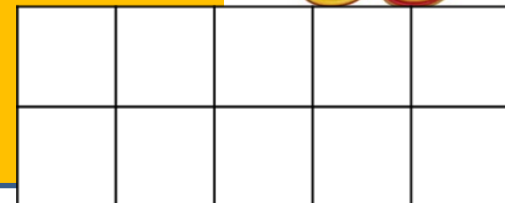
Example: $19 - 13 = 6$



Resources:

- Tens Frames
- Two sided counters
- Dienes

Practical first!



Subtraction Formal Written Methods for Calculation

Year 2

Subtract ones from a two-digit number.

Subtract tens from a two-digit number.

Subtract one two-digit number from another.

Resources:

- Dienes

Practical + Pictorial

a) $49 - 6 = 43$

b) $24 - 9 = 15$

c) $45 - 20 = 25$

d) $45 - 33 = 12$

e) $63 - 28 = 35$

Abstract

Short Column Written Method

Two-digit - single digit (not breaking 10)

a) $49 - 6 = 43$

$$\begin{array}{r} 49 \\ - 6 \\ \hline 43 \end{array}$$

Two-digit - single digit (breaking 10)

b) $34 - 9 = 25$

$$\begin{array}{r} 34 \\ - 9 \\ \hline 25 \end{array}$$

Two-digit - tens

c) $45 - 20 = 25$

$$\begin{array}{r} 45 \\ - 20 \\ \hline 25 \end{array}$$

Two-digit - two-digit (not breaking 10)

d) $45 - 33 = 12$

$$\begin{array}{r} 45 \\ - 33 \\ \hline 12 \end{array}$$

Two-digit - two-digit (breaking 10)

e) $63 - 28 = 35$

$$\begin{array}{r} 63 \\ - 28 \\ \hline 35 \end{array}$$

National curriculum expectations

Subtraction

Year 3

Subtract numbers with up to 3 digits using formal written methods of columnar subtraction.

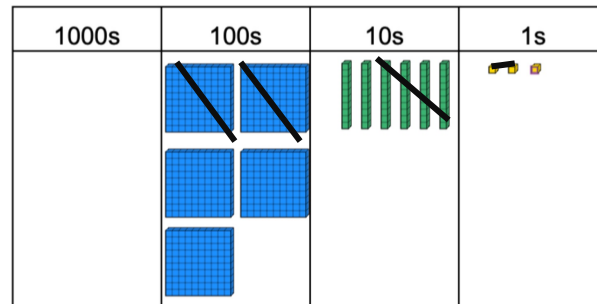
Resources:

- Dienes

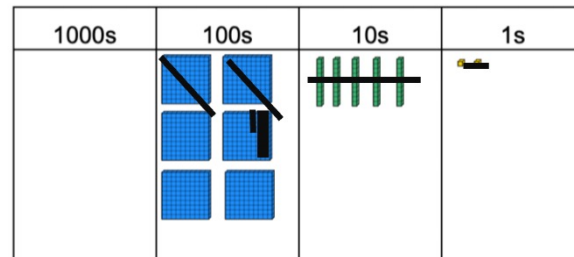
Subtraction Formal Written Methods for Calculation

Practical + Pictorial

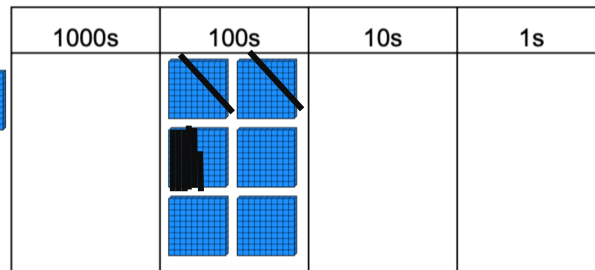
$$563 - 241 = 322$$



$$652 - 287 =$$



$$600 - 255 = 345$$



Abstract

Short Column Written Method

3-digit - 3-digit

$$563 - 241 = 322$$

$$\begin{array}{r} 563 \\ - 241 \\ \hline 322 \end{array}$$

$$652 - 287 = 365$$

$$\begin{array}{r} 5 \quad 14 \\ 6 \quad 5 \quad 12 \\ - 2 \quad 8 \quad 7 \\ \hline 3 \quad 6 \quad 5 \end{array}$$

$$600 - 255 = 345$$

$$\begin{array}{r} 5 \quad 9 \\ 6 \quad 10 \quad 10 \\ - 2 \quad 5 \quad 5 \\ \hline 3 \quad 4 \quad 5 \end{array}$$

Don't forget mixed digit whole number questions

Year 4

Subtract numbers with up to 4 digits using the formal written methods of columnar subtraction.

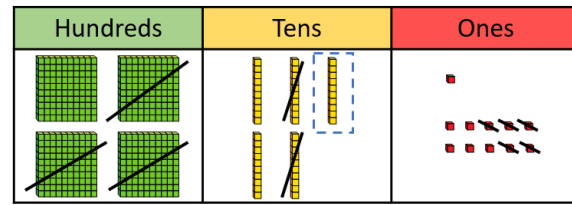
Resources:

- Dienes
- Place Value Mats (Progressive)

Subtraction Formal Written Methods for Calculation

Practical + Pictorial

$$451 - 325 = 126$$



Thousands	Hundreds, Tens and Ones			Decimals	
Thousands 1 000	Hundreds 100	Tens 10	Ones 1	Tenths 0.1	Hundredths 0.01
7	5	1	3		
- 3	2	7	8		
4	2	2	5		

Thousands	Hundreds, Tens and Ones			Decimals	
Thousands 1 000	Hundreds 100	Tens 10	Ones 1	Tenths 0.1	Hundredths 0.01
5	9	9	1		
- 2	5	4	3		
3	4	5	7		

Abstract

Short Column Written Method

4-digit + 4-digit

a) $8,469 - 2,127 = 6,342$

$$\begin{array}{r} 8 \quad 4 \quad 6 \quad 9 \\ - 2 \quad 1 \quad 2 \quad 7 \\ \hline 6 \quad 3 \quad 4 \quad 2 \end{array}$$

b) $7,503 - 3,278 = 4,225$

$$\begin{array}{r} 7 \quad 5 \quad 0 \quad 3 \\ - 3 \quad 2 \quad 7 \quad 8 \\ \hline 4 \quad 2 \quad 2 \quad 5 \end{array}$$

c) $6,000 - 2,543 = 3,457$

$$\begin{array}{r} 6 \quad 0 \quad 0 \quad 0 \\ - 2 \quad 5 \quad 4 \quad 3 \\ \hline 3 \quad 4 \quad 5 \quad 7 \end{array}$$

Don't forget mixed digit whole number questions

Year 5 + 6

Subtract whole numbers with more than 4 digits including using formal written methods (columnar subtraction).

Practise subtracting decimals, including a mix of whole numbers and decimals, followed by decimals with different numbers of decimal places.

Resources:

- Dienes
- Place Value Mats (Progressive)

Subtraction Formal Written Methods for Calculation

Practical + Pictorial

a) $52,849 - 18,423 = 34,426$

Millions			Thousands			Hundreds, Tens and Ones			Decimals		
Hundred Millions	Ten Millions	Millions	Hundred thousands	Ten thousands	Thousands	Hundreds	Tens	Ones	Tenths	Hundredths	Thousandths
			5	2	8	4	9				
			1	8	4	2	3				
			3	4	4	2	6				

b) $2,000,000 - 287,941 = 1,712,059$

Millions			Thousands			Hundreds, Tens and Ones			Decimals		
Hundred Millions	Ten Millions	Millions	Hundred thousands	Ten thousands	Thousands	Hundreds	Tens	Ones	Tenths	Hundredths	Thousandths
		2	0	0	0	0	0	0			
			2	8	7	9	4	1			
			1	7	1	2	0	5			

d) $14 - 3.692 = 10.308$

Millions			Thousands			Hundreds, Tens and Ones			Decimals		
Hundred Millions	Ten Millions	Millions	Hundred thousands	Ten thousands	Thousands	Hundreds	Tens	Ones	Tenths	Hundredths	Thousandths
							1	4			
							3		6	9	2
							1	0	3	0	8

Abstract

Short Column Written Method

More than 4-digit + 4-digit whole numbers

a) $52,849 - 18,423 = 34,426$

$$\begin{array}{r} 52,849 \\ - 18,423 \\ \hline 34,426 \end{array}$$

b) $2,000,000 - 287,941 = 1,712,059$

$$\begin{array}{r} 2,000,000 \\ - 287,941 \\ \hline 1,712,059 \end{array}$$

With decimals

c) $63.75 - 17.28 = 46.47$

$$\begin{array}{r} 63.75 \\ - 17.28 \\ \hline 46.47 \end{array}$$

d) $14 - 3.692 = 10.308$

$$\begin{array}{r} 14 \\ - 3.692 \\ \hline 10.308 \end{array}$$

Add in place holders to 'box' the subtraction.

Don't forget mixed digit whole number questions

Subtraction Formal Written Methods for Calculation

National curriculum expectations

Subtraction

Column method

Year 2

- Subtract ones from a two-digit number.
- Subtract tens from a two-digit number.
- Subtract one two-digit number from another.

2-digit - 2-digit

$$74 - 23 = 51$$

$$\begin{array}{r} 74 \\ - 23 \\ \hline 51 \end{array}$$

$$63 - 48 = 15$$

$$\begin{array}{r} 63 \\ - 48 \\ \hline 15 \end{array}$$

Year 3

- Subtract numbers with up to 3 digits using formal written methods of columnar subtraction.

3-digit - 3-digit

$$563 - 241 = 322$$

$$\begin{array}{r} 563 \\ - 241 \\ \hline 322 \end{array}$$

$$652 - 287 = 365$$

$$\begin{array}{r} 652 \\ - 287 \\ \hline 365 \end{array}$$

$$600 - 255 = 345$$

$$\begin{array}{r} 600 \\ - 255 \\ \hline 345 \end{array}$$

Year 4

- Subtract numbers with up to 4 digits using the formal written methods of columnar subtraction.

4-digit - 4-digit

$$8469 - 2127 = 6342$$

$$\begin{array}{r} 8469 \\ - 2127 \\ \hline 6342 \end{array}$$

$$7503 - 3278 = 4225$$

$$\begin{array}{r} 7503 \\ - 3278 \\ \hline 4225 \end{array}$$

$$6000 - 2543 = 3457$$

$$\begin{array}{r} 6000 \\ - 2543 \\ \hline 3457 \end{array}$$

Year 5 and Year 6

- Subtract whole numbers with more than 4 digits including using formal written methods (columnar subtraction).

Practise subtracting decimals, including a mix of whole numbers and decimals, followed by decimals with different numbers of decimal places.

$$52,849 - 18,423 = 34,426$$

$$\begin{array}{r} 52849 \\ - 18423 \\ \hline 34426 \end{array}$$

$$2,000,000 - 287,941 = 1,712,059$$

$$\begin{array}{r} 2000000 \\ - 287941 \\ \hline 1712059 \end{array}$$

With decimals

$$63.75 - 17.28 = 46.47$$

$$\begin{array}{r} 63.75 \\ - 17.28 \\ \hline 46.47 \end{array}$$

$$14 - 3.692 = 10.308$$

$$\begin{array}{r} 14.000 \\ - 3.692 \\ \hline 10.308 \end{array}$$

Add in place holders to 'box' the subtraction.

Year 3

Multiply 2 numbers by a 1 digit number using a formal written layout.

Pupils practise to become fluent in the formal written method of short multiplication using the times tables they know.







Resources:

- Dienes









Multiplication Formal Written Methods for Calculation

Practical + Pictorial

$$34 \times 3 = 102$$

Tens	Ones
	
	
	

$$24 \times 4 = 96$$

Tens	Ones
	
	
	
	

Abstract

Short Method
2 x 1 examples

$$21 \times 4 = 84$$

$$\begin{array}{r} 21 \\ \times 4 \\ \hline 84 \end{array}$$

$$14 \times 5 = 70$$

$$\begin{array}{r} 14 \\ \times 5 \\ \hline 70 \\ 2 \end{array}$$

$$34 \times 8 = 272$$

$$\begin{array}{r} 34 \\ \times 8 \\ \hline 272 \\ 23 \end{array}$$

Year 4

Multiply 2 and 3 digit numbers by a 1 digit number using a formal written layout.

Pupils consolidate their fluency in the formal written method of short multiplication using all times tables facts.

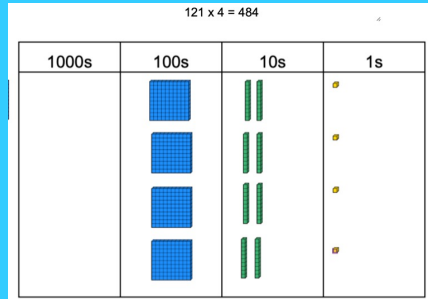
Resources:

- Dienes
- Place Value Mats (Progressive)

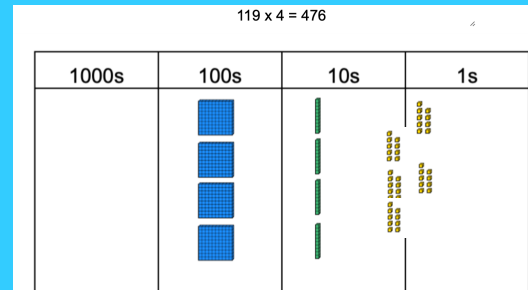
Multiplication Formal Written Methods for Calculation

Practical + Pictorial

$$121 \times 4 = 484$$



$$119 \times 4 = 476$$



$$456 \times 7 = 3192$$

Thousands	Hundreds, Tens and Ones		
Thousands 1,000	Hundreds 100	Tens 10	Ones 1
	4	5	6
X			7
	3	1	9
	3	3	4

Abstract

Short Method

3 x 1 examples

$$121 \times 4 = 484$$

$$\begin{array}{r} 121 \\ \times \quad 4 \\ \hline 484 \end{array}$$

$$119 \times 4 = 476$$

$$\begin{array}{r} 119 \\ \times \quad 4 \\ \hline 476 \\ 3 \end{array}$$

$$456 \times 7 = 3192$$

$$\begin{array}{r} 456 \\ \times \quad 7 \\ \hline 3192 \\ 334 \end{array}$$

Year 5

Multiply numbers up to 4 digits by a 1 or 2 digit number using a formal written method, including long multiplication for 2 digit numbers.

Resources:

- Place Value Mats (Progressive)

Multiplication Formal Written Methods for Calculation

Practical + Pictorial

a) $1234 \times 4 = 4936$

Millions			Thousands			Hundreds, Tens and Ones		
Hundred Millions 100 000 000	Ten Millions 10 000 000	Millions 1 000 000	Hundred thousands 100 000	Ten thousands 10 000	Thousands 1 000	Hundreds 100	Tens 10	Ones 1
					1	2	3	4
					4	9	3	6
						1	1	

b) $24 \times 16 = 384$

Millions			Thousands			Hundreds, Tens and Ones		
Hundred Millions 100 000 000	Ten Millions 10 000 000	Millions 1 000 000	Hundred thousands 100 000	Ten thousands 10 000	Thousands 1 000	Hundreds 100	Tens 10	Ones 1
						2	4	
						1	6	
					1	4	4	
						2		
					2	4	0	
					3	8	4	

Abstract**Short Method
4 x 1 example**

$1234 \times 4 = 4936$

$$\begin{array}{r}
 24 \\
 \times 24 \\
 \hline
 436 \\
 \hline
 4936
 \end{array}$$

**Long Multiplication
2 x 2 example**

$24 \times 16 = 384$

$$\begin{array}{r}
 4 \\
 \times 16 \\
 \hline
 144 \\
 240 \\
 \hline
 384
 \end{array}$$

Year 6

Multiply multi-digit numbers up to 4 digits by a 2 digit whole number using the formal written method of long multiplication.

Multiply 1 digit numbers with up to 2 decimal places by whole numbers.

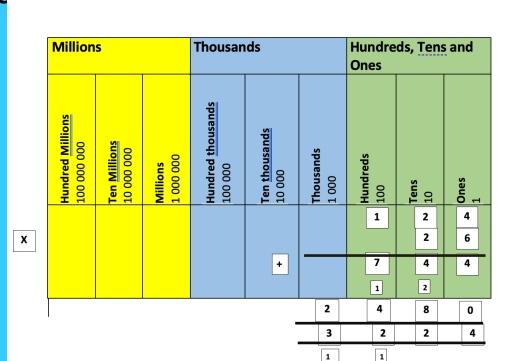
Resources:

- Place Value Mats (Progressive)

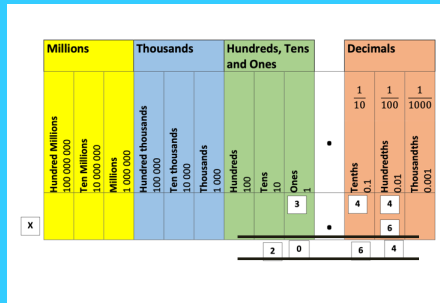
Multiplication Formal Written Methods for Calculation

Practical + Pictorial

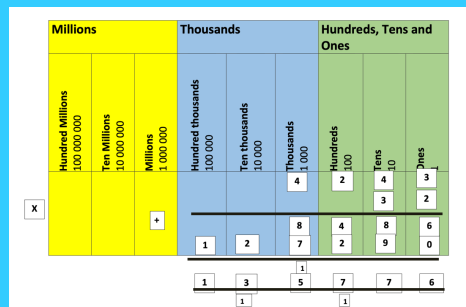
a) $124 \times 26 = 3224$



b) $3.44 \times 6 = 20.64$



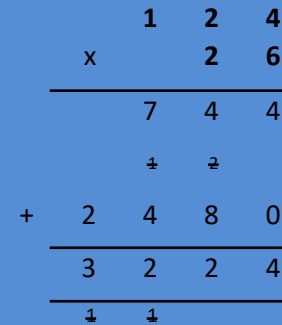
c) $4243 \times 32 = 135,776$



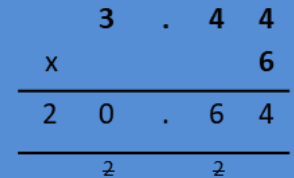
Abstract

**Long Multiplication
3 x 2 example**

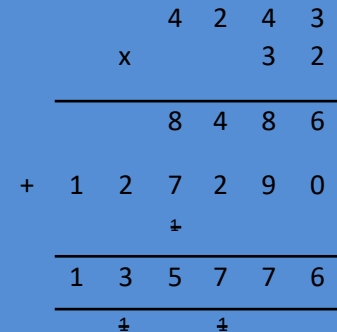
$124 \times 26 = 3224$



**Multiplying decimals
(Short method)**



**Long Multiplication
4 x 2 example**



Multiplication Formal Written Methods for Calculation

National curriculum expectations

Multiplication

Year 2

Calculate mathematical statements for multiplication within the multiplication tables and write them using the signs \times and $=$

Number Statements

$$6 \times 5 = 30$$

$$5 \times 6 = 30$$

$$8 \times 2 = 16$$

$$2 \times 8 = 16$$

Year 3

Multiply 2 numbers by a 1 digit number using a formal written layout.

Pupils practise to become fluent in the formal written method of short multiplication using the times tables they know.

Short Method 2 x 1 examples

$$21 \times 4 = 84$$

$$\begin{array}{r} 21 \\ \times 4 \\ \hline 84 \end{array}$$

$$14 \times 5 = 70$$

$$\begin{array}{r} 14 \\ \times 5 \\ \hline 70 \end{array}$$

$$34 \times 8 = 272$$

$$\begin{array}{r} 34 \\ \times 8 \\ \hline 272 \end{array}$$

Year 4

Multiply 2 and 3 digit numbers by a 1 digit number using a formal written layout.

Pupils consolidate their fluency in the formal written method of short multiplication using all times tables facts.

Short Method 3 x 1 examples

$$121 \times 4 = 484$$

$$\begin{array}{r} 121 \\ \times 4 \\ \hline 484 \end{array}$$

$$119 \times 4 = 476$$

$$\begin{array}{r} 119 \\ \times 4 \\ \hline 476 \end{array}$$

$$456 \times 7 = 3192$$

$$\begin{array}{r} 456 \\ \times 7 \\ \hline 3192 \end{array}$$

Year 5 and Year 6

Multiply numbers up to 4 digits by a 1 or 2 digit number using a formal written method, including long multiplication for 2 digit numbers.

Short Method 4 x 1 example

$$\begin{array}{r} 1234 \\ \times 4 \\ \hline 4936 \end{array}$$

Multiplying decimals (Short method)

$$\begin{array}{r} 3.44 \\ \times 6 \\ \hline 20.64 \end{array}$$

Long Multiplication 2 x 2 example

$$\begin{array}{r} 24 \\ \times 16 \\ \hline 144 \\ 240 \\ \hline 384 \end{array}$$

Multiply multi-digit numbers up to 4 digits by a 2 digit whole number using the formal written method of long multiplication.

Multiply 1 digit numbers with up to 2 decimal places by whole numbers.

Long Multiplication 3 x 2 example

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ + 2480 \\ \hline 3224 \end{array}$$

4 x 2 example

$$\begin{array}{r} 4243 \\ \times 32 \\ \hline 8486 \\ + 127290 \\ \hline 135776 \end{array}$$

Division Formal Written Methods for Calculation

Year 3

National curriculum expectations

Write and calculate mathematical statements for division using the multiplication tables that they know, including for 2 digit numbers times 1 digit numbers.

Pupils develop reliable written methods for division starting with calculations of 2 digit by 1 digit and progression to the formal written methods of short division.

Resources:

- Dienes

Practical + Pictorial

a)

1000s	100s	10s	1s

$69 \div 3 = 23$

1000s	100s	10s	1s

$65 \div 5 = 13$

Abstract

Short Method: 2 x 1 examples

$69 \div 3 = 23$

$$\begin{array}{r} 23 \\ 3 \overline{) 69} \end{array}$$

$65 \div 5 = 13$

$$\begin{array}{r} 13 \\ 5 \overline{) 65} \end{array}$$

$92 \div 4 = 23$

$$\begin{array}{r} 23 \\ 4 \overline{) 92} \end{array}$$

Division

Division Formal Written Methods for Calculation

Year 4

National curriculum expectations

Pupils practise to become fluent in the formal written method of short division with exact answers. (Up to 3 by 1)

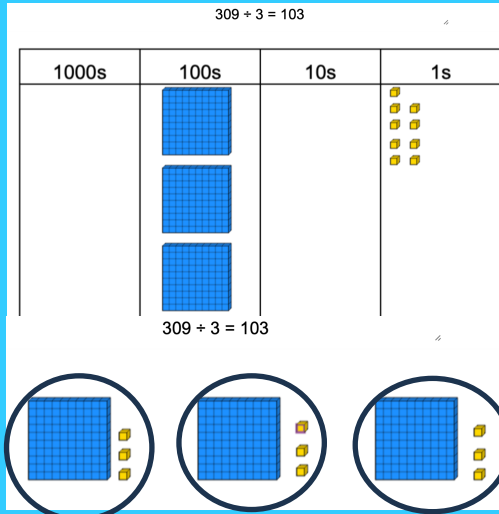
Resources:

- Dienes

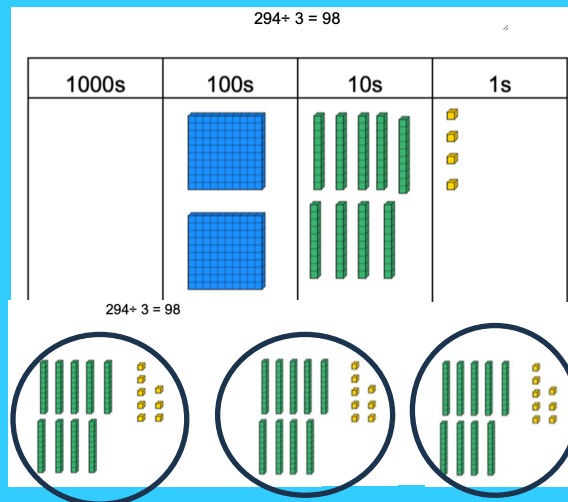
Division

Practical + Pictorial

a) $309 \div 3 = 103$



b) $294 \div 3 = 98$



Abstract

Short Method: 3 x 1 examples

$309 \div 3 = 103$

$$\begin{array}{r} 103 \\ 3 \overline{) 309} \\ \underline{3} \\ 0 \\ \underline{ 0} \\ 9 \\ \underline{ 9} \\ 0 \end{array}$$

$896 \div 4 = 224$

$$\begin{array}{r} 224 \\ 4 \overline{) 896} \\ \underline{8} \\ 9 \\ \underline{ 8} \\ 6 \\ \underline{ 6} \\ 0 \end{array}$$

$294 \div 3 = 98$

$$\begin{array}{r} 98 \\ 3 \overline{) 294} \\ \underline{2} \\ 9 \\ \underline{ 9} \\ 4 \\ \underline{ 4} \\ 0 \end{array}$$

Year 5

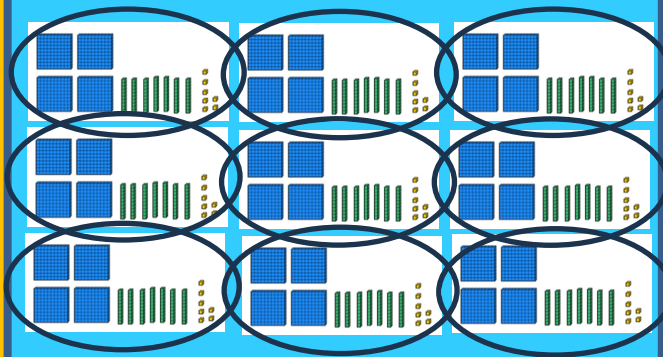
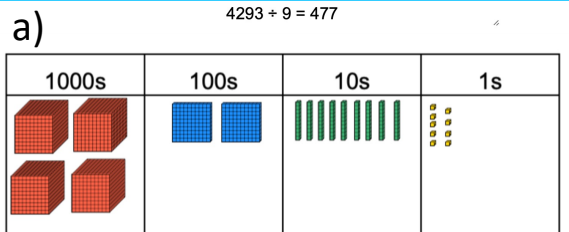
Divide numbers up to 4 digits by a 1 digit number using the formal written method of short division and interpret remainders appropriately for the context.

Resources:

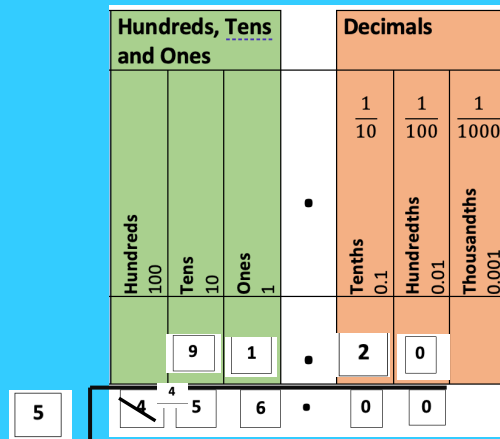
- Dienes
- Place Value Mats (Progressive)

Division Formal Written Methods for Calculation

Practical + Pictorial



b)



Abstract

Short Method

4 x 1 example

$$4293 \div 9 = 477$$

$$\begin{array}{r} 0 \quad 4 \quad 7 \quad 7 \\ 9 \overline{) 4 \quad 2 \quad 9 \quad 3} \\ \underline{4 \quad 2} \quad \quad \quad \\ \quad \quad 9 \quad \quad \quad \\ \underline{\quad \quad 9} \quad \quad \quad \\ \quad \quad \quad 0 \quad \quad \quad \\ \quad \quad \quad \quad 3 \quad \quad \quad \\ \underline{\quad \quad \quad 3} \quad \quad \quad \\ \quad \quad \quad \quad \quad 0 \quad \quad \quad \end{array}$$

Short Method that will have a decimal remainder
e.g. $\pounds 456 \div 5 = \pounds 91.20$

$$\begin{array}{r} 0 \quad 9 \quad 1 \quad . \quad 2 \\ 5 \overline{) 4 \quad 5 \quad 6 \quad . \quad 0} \\ \underline{4 \quad 5} \quad \quad \quad \\ \quad \quad 6 \quad \quad \quad \\ \underline{\quad \quad 6} \quad \quad \quad \\ \quad \quad \quad 0 \quad \quad \quad \\ \quad \quad \quad \quad 0 \quad \quad \quad \\ \underline{\quad \quad \quad 0} \quad \quad \quad \\ \quad \quad \quad \quad \quad 0 \quad \quad \quad \end{array}$$

$$\pounds 456 \div 5 = \pounds 91.20$$

Additional place holder for the quotient as money always has 2 decimal places.

Year 6

Divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.

Divide numbers up to 4 digits by a 2 digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.

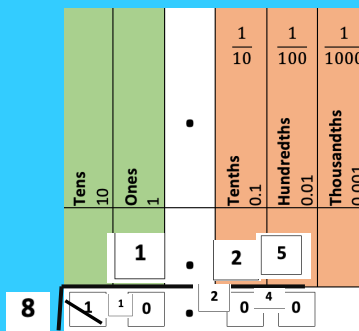
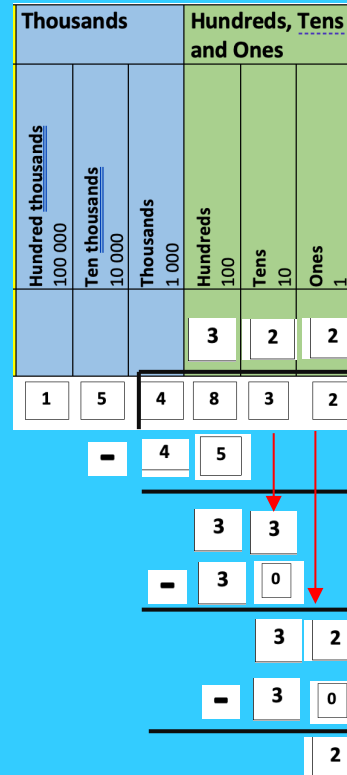
Pupils are introduced to the division of decimal numbers by 1 digit whole number, initially, in practical contexts involving measures and money.

Resources:

- Dienes
- Place Value Mats (Progressive)

Division Formal Written Methods for Calculation

Practical + Pictorial



Abstract

Long Division 4 x 2 example
 $4832 \div 15 = 322 \text{ r } 2$

$$\begin{array}{r}
 15 \overline{) 4832} \\
 \underline{48} \\
 30 \\
 \underline{30} \\
 20 \\
 \underline{20} \\
 2
 \end{array}$$

Short Division 4 x 2 example
 $4268 \div 22 = 194$

$$\begin{array}{r}
 22 \overline{) 4268} \\
 \underline{42} \\
 206 \\
 \underline{206} \\
 8
 \end{array}$$

Short Method decimal by single digit
 $267.75 \div 5 = 53.55$

$$\begin{array}{r}
 5 \overline{) 267.75} \\
 \underline{20} \\
 26 \\
 \underline{25} \\
 17 \\
 \underline{15} \\
 27 \\
 \underline{25} \\
 25
 \end{array}$$

Short Method Whole number by single digit with decimal quotient
 $10 \div 8 = 1.25$

Additional place holders needed here.

$$\begin{array}{r}
 8 \overline{) 10.25} \\
 \underline{8} \\
 20 \\
 \underline{16} \\
 40 \\
 \underline{40} \\
 0
 \end{array}$$

Division Formal Written Methods for Calculation

National curriculum expectations

Division

Year 2

Calculate mathematical statements for division within the multiplication tables and write them using the signs \div and $=$

Number Statements

$$6 \div 2 = 3$$

$$20 \div 5 = 4$$

$$18 \div 2 = 9$$

Year 3

Write and calculate mathematical statements for division using the multiplication tables that they know, including for 2 digit numbers times 1 digit numbers.

Pupils develop reliable written methods for division starting with calculations of 2 digit by 1 digit and progression to the formal written methods of short division.

Short Method: 2 x 1 example

$$92 \div 4 = 23$$

$$\begin{array}{r} 23 \\ 4 \overline{) 92} \\ \underline{8} \\ 12 \\ \underline{12} \\ 0 \end{array}$$

Year 4

Pupils practise to become fluent in the formal written method of short division with exact answers.

Short Method: 3 x 1 example

$$294 \div 3 = 98$$

$$\begin{array}{r} 98 \\ 3 \overline{) 294} \\ \underline{6} \\ 29 \\ \underline{27} \\ 24 \\ \underline{24} \\ 0 \end{array}$$

Year 5

Divide numbers up to 4 digits by a 1 digit number using the formal written method of short division and interpret remainders appropriately for the context.

Short Method 4 x 1 example

$$4293 \div 9 = 477$$

$$\begin{array}{r} 477 \\ 9 \overline{) 4293} \\ \underline{36} \\ 69 \\ \underline{63} \\ 63 \\ \underline{63} \\ 0 \end{array}$$

Short Method that will have a decimal remainder
e.g. $\pounds 456 \div 5 = \pounds 91.20$

$$\begin{array}{r} 91.20 \\ 5 \overline{) 456.20} \\ \underline{20} \\ 25 \\ \underline{25} \\ 0 \\ \underline{0} \\ 20 \\ \underline{20} \\ 0 \end{array}$$

$$\pounds 456 \div 5 = \pounds 91.20$$

Additional place holder for the quotient as money always has 2 decimal places.

Year 6

Divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.

Divide numbers up to 4 digits by a 2 digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.

Pupils are introduced to the division of decimal numbers by 1 digit whole number, initially, in practical contexts involving measures and money.

$$10 \div 8 = 1.25$$

Additional place holders needed here.

Long Division 4 x 2 example

$$4832 \div 15 = 322 \text{ r } 2$$

$$\begin{array}{r} 322 \\ 15 \overline{) 4832} \\ \underline{45} \\ 33 \\ \underline{30} \\ 20 \\ \underline{15} \\ 50 \\ \underline{45} \\ 52 \\ \underline{45} \\ 72 \\ \underline{60} \\ 12 \end{array}$$

Short Division 4 x 2 example

$$4268 \div 22 = 194$$

$$\begin{array}{r} 194 \\ 22 \overline{) 4268} \\ \underline{44} \\ 68 \\ \underline{66} \\ 28 \\ \underline{22} \\ 68 \\ \underline{66} \\ 28 \end{array}$$

Short Method Decimal by single digit

$$267.75 \div 5 = 53.55$$

$$\begin{array}{r} 53.55 \\ 5 \overline{) 267.75} \\ \underline{25} \\ 17 \\ \underline{15} \\ 27 \\ \underline{25} \\ 25 \\ \underline{25} \\ 0 \end{array}$$

Short Method Whole number by single digit with decimal quotient

$$\begin{array}{r} 1.25 \\ 8 \overline{) 10.25} \\ \underline{8} \\ 20 \\ \underline{16} \\ 40 \\ \underline{40} \\ 0 \end{array}$$